



Modeling Student Mobility Using Hierarchical Networks

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Multilevel Conference, April, 2019



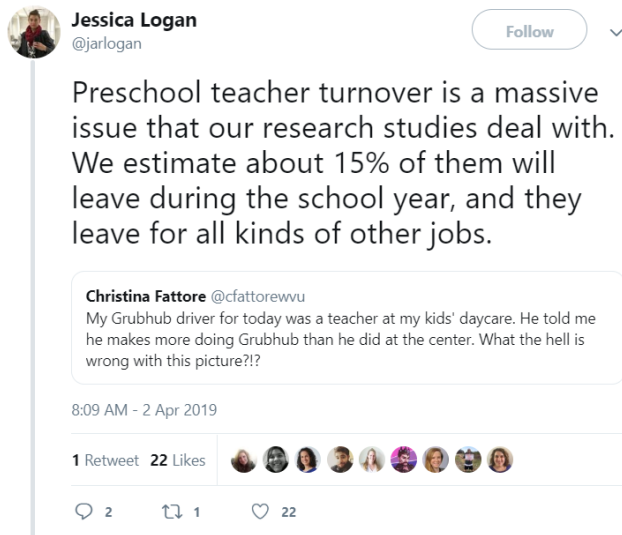
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Acknowledgement

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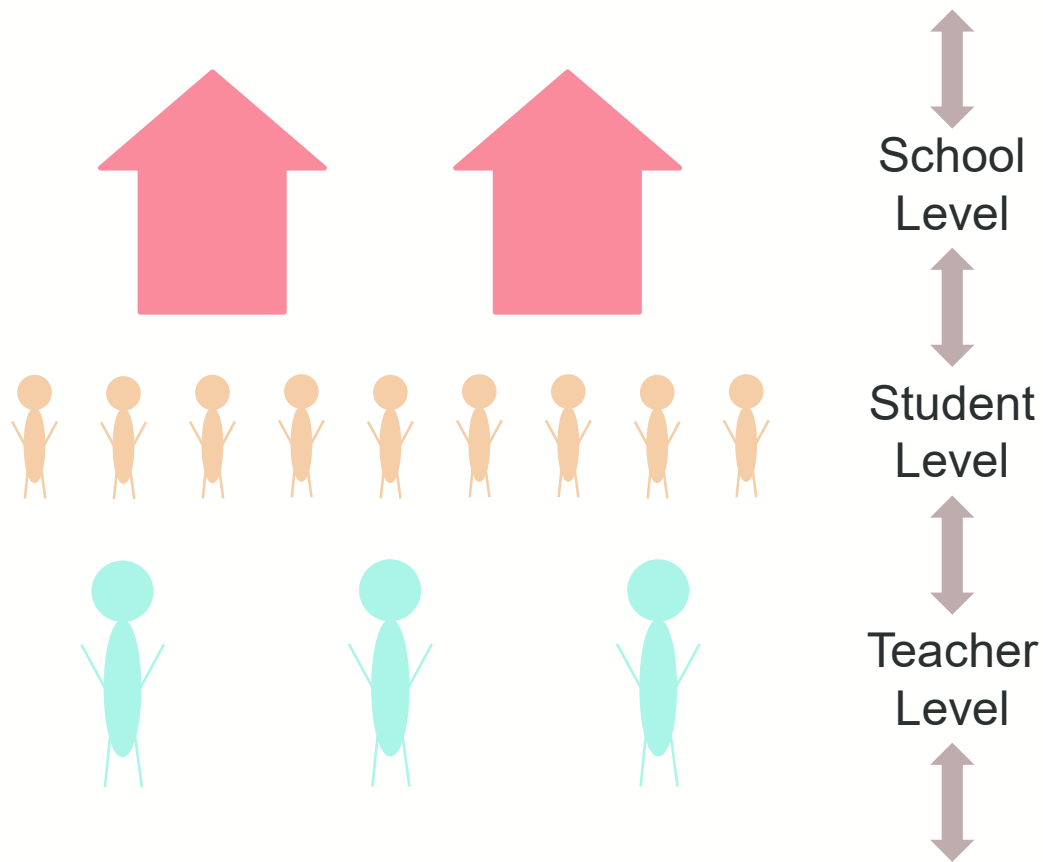
Overview

- “Mobility” is a complex and ongoing issue in education settings



Piasta, S. B., Logan, J. A. R., Pelatti, C. Y., & Capps, J. L. (2015). Professional development for early childhood educators: Efforts to improve math and science learning opportunities in early childhood classrooms. *Journal of Educational Psychology*, 107(2), 407-422.

Overview



Overview

- Common modeling procedures to handle mobility in education:
 - Multiple membership random effects model (MMREM; Browne, Goldstein, & Rasbash, 2001)
 - Use observed student mobility as a predictor or outcome in regression
 - Ignore it!

Overview

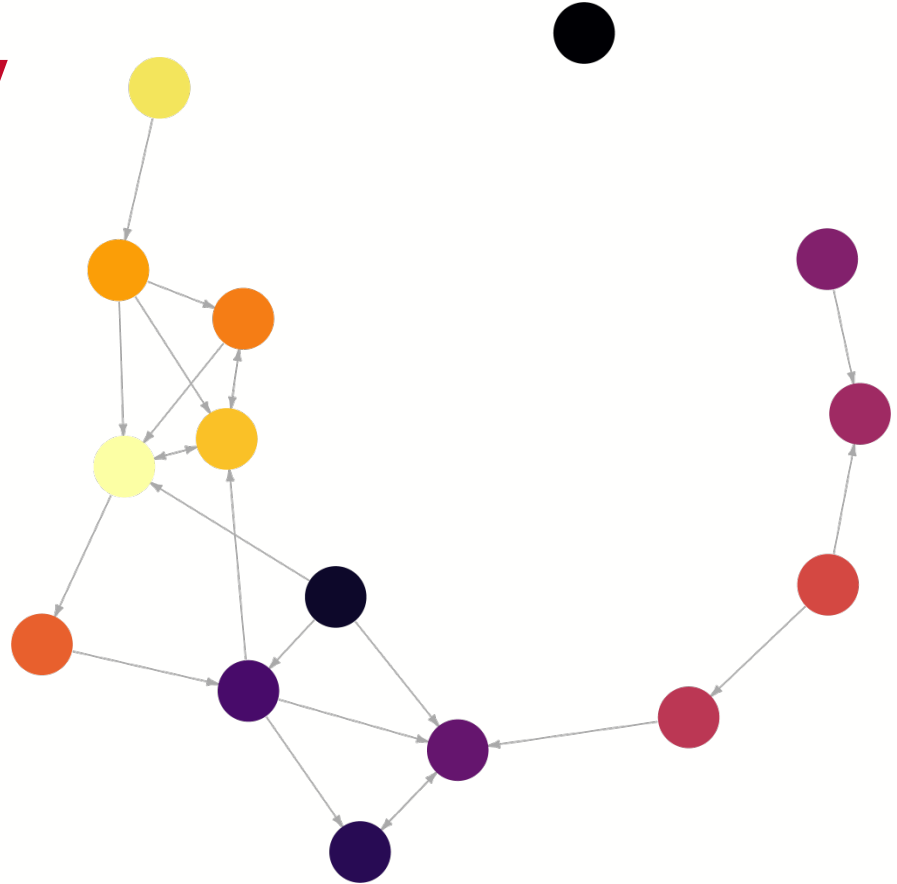
- We propose an alternative approach—multilevel network analysis
- Our findings, in brief:
 - Network models are capable of handling the complex dependencies among schools
 - Real data may contain few cluster-level observations and few nodes within clusters, which is problematic for estimation

Outline

- Introduction to mobility
- Social network modeling methods
- Results from the real data illustration
- Where do we go from here?

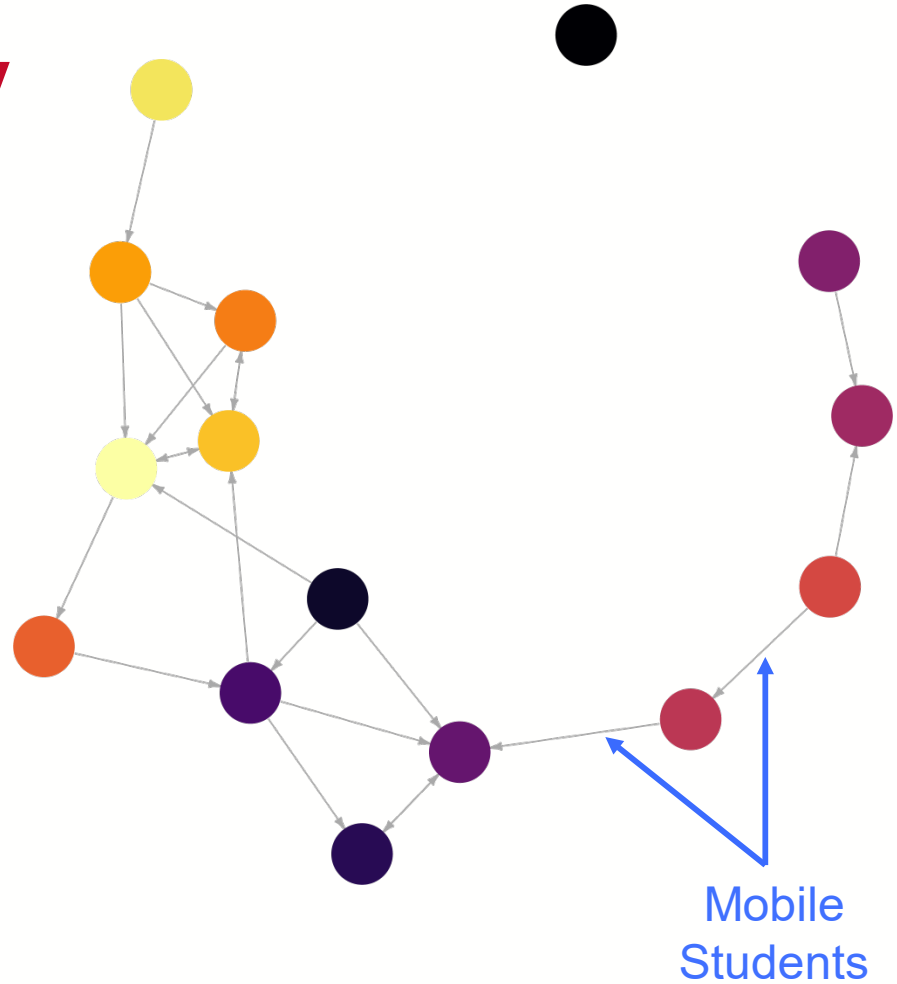
Patterns of Mobility

Students are mobile...but in a particular way



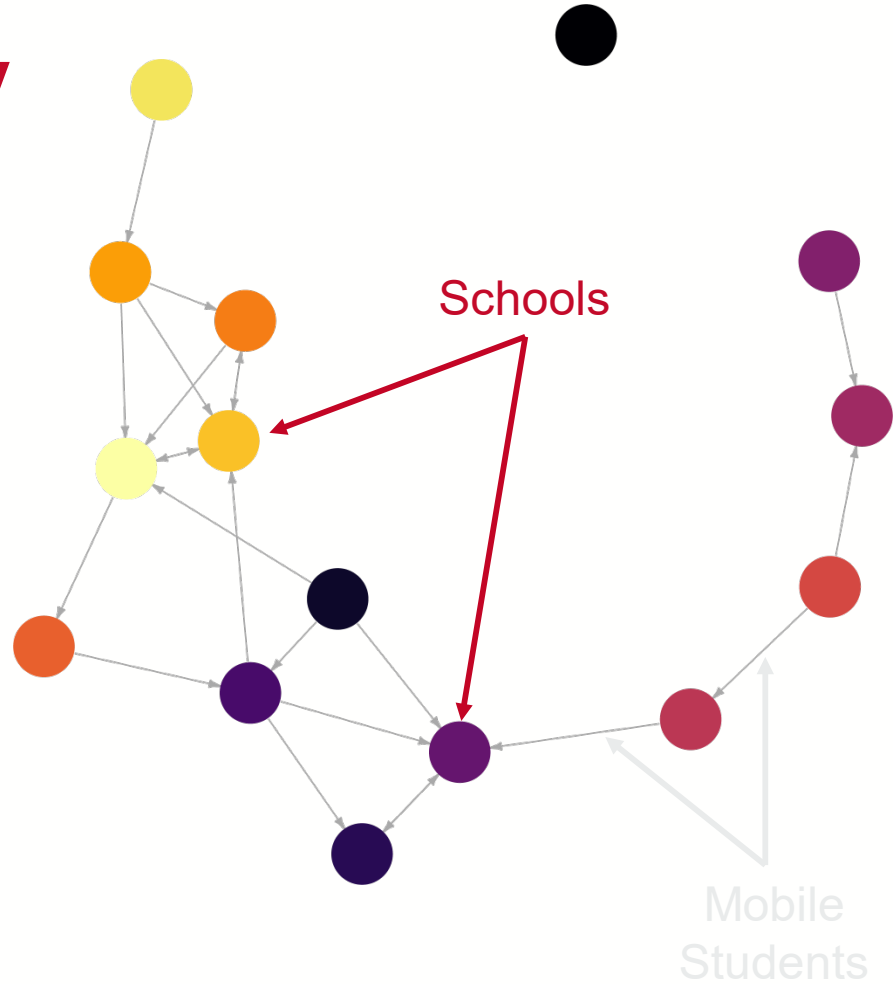
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Patterns of Mobility

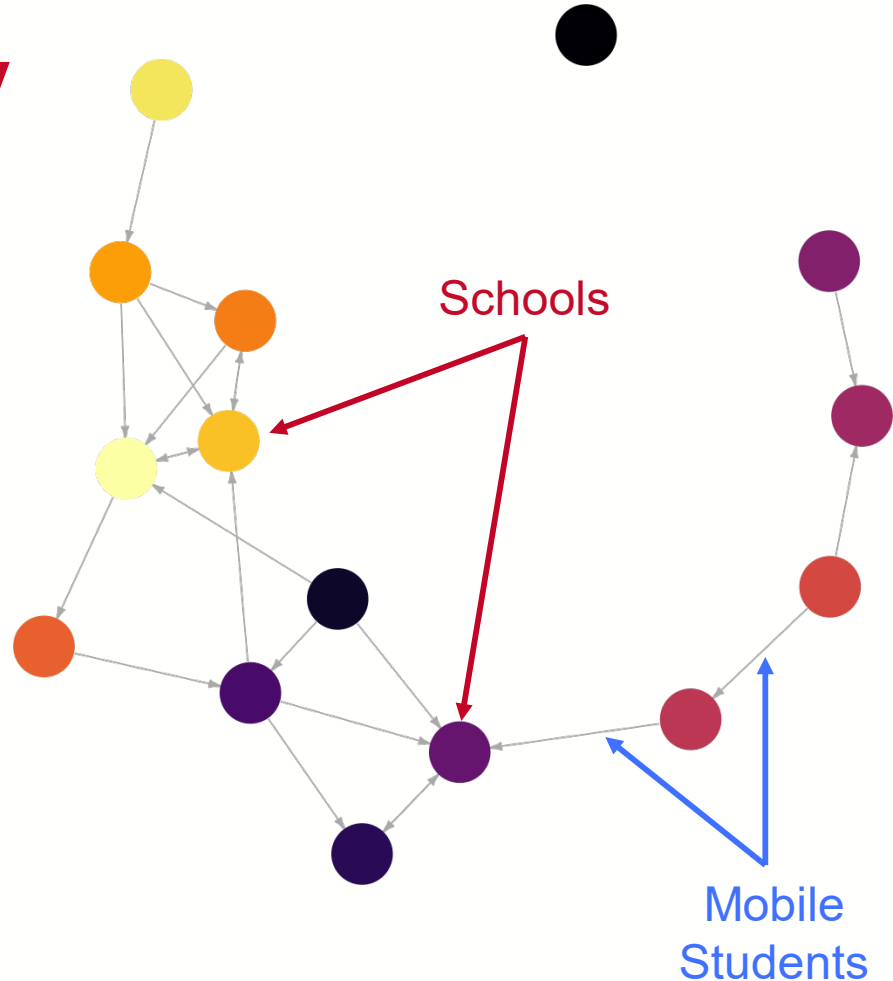
Students are mobile...but in a particular way



Patterns of Mobility

Students are mobile...but in a particular way

- Current “best practices” recommendations in education indicate the use of MMREMs
- MMREMs are problematic because they don’t account for complex relations among schools



Multiple Membership Model

$$\omega \sim N\left(Z_W \cdot \beta, \tau_{00} \right)$$
$$y \sim N\left(\omega + X \cdot \gamma, \sigma^2 \right)$$

- Weights are often assigned (not estimated) as $1/H$, where H is the number of schools attended by student i
- A naive, first-school approach is a special case of this model where the first school is given a weight of 1 and subsequent school weights are set at 0
- Z_W is constructed as $w_{i,1}^* z_{p,1} + \dots + w_{i,H}^* z_{p,H}$ - assumes 0 correlation between schools

What do real data tell us? (SAT Math)

Correlations Among School Residuals (J=266)

1. N = 15926

2. N = 15185

3. N = 3902

1. First School Attended

—

2. Second School Attended

0.479

—

3. Third School Attended

0.396

0.392

—

What do real data tell us? (HS Algebra)

Correlations Among School Residuals (J=266)

1. N = 15926

2. N = 15185

3. N = 3902

1. First School Attended

—

2. Second School Attended

0.432

—

3. Third School Attended

0.359

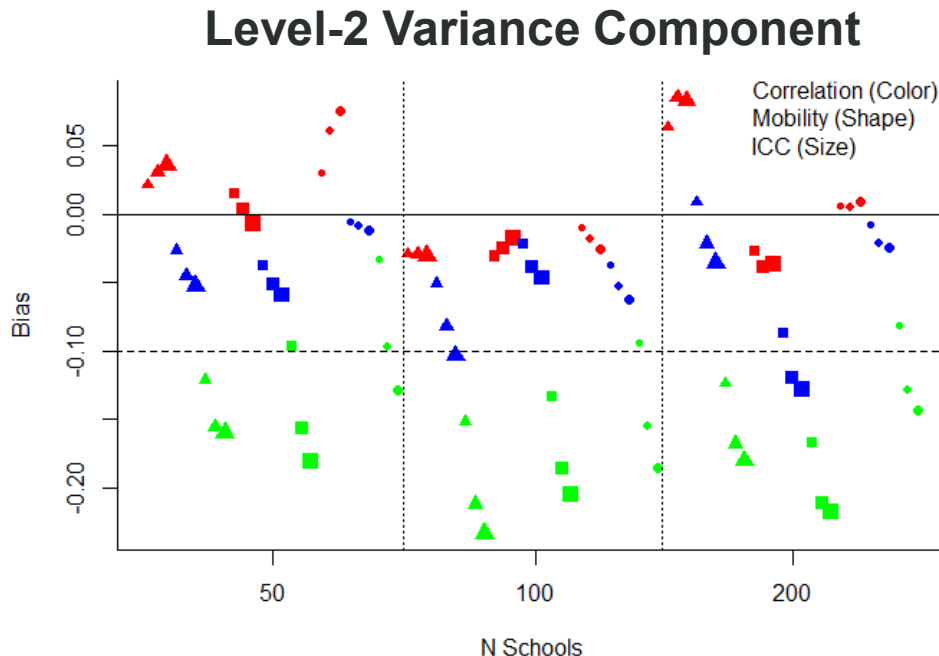
0.375

—

What do simulations tell us?

Where do MMREMs fail?

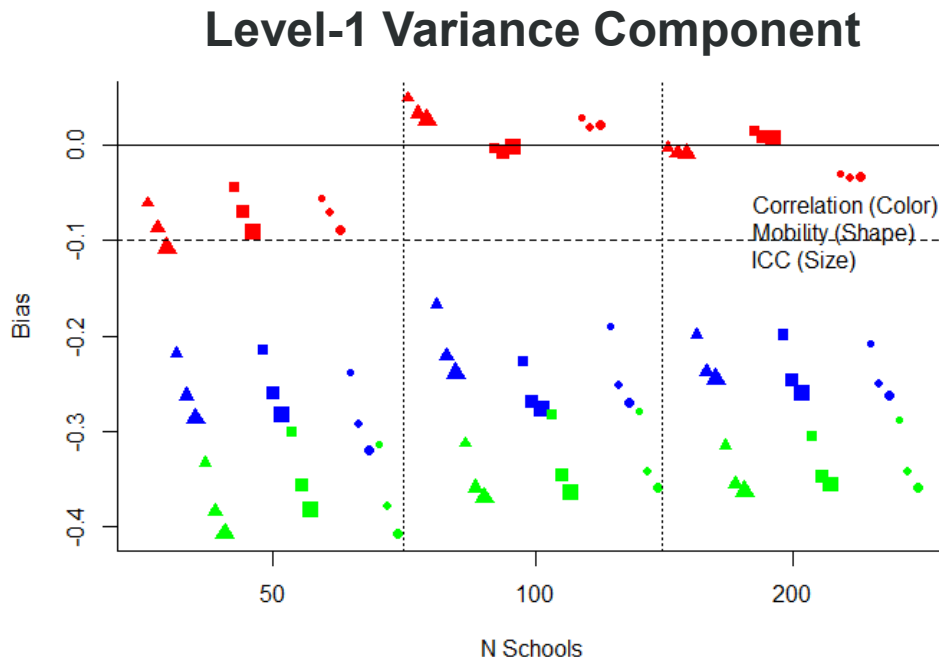
- High Correlation (all)
- Gets worse with increasing ICC



What do simulations tell us?

Where do MMREMs fail?

- High Correlations (0.25, 0.50)
- Gets worse with increasing ICC



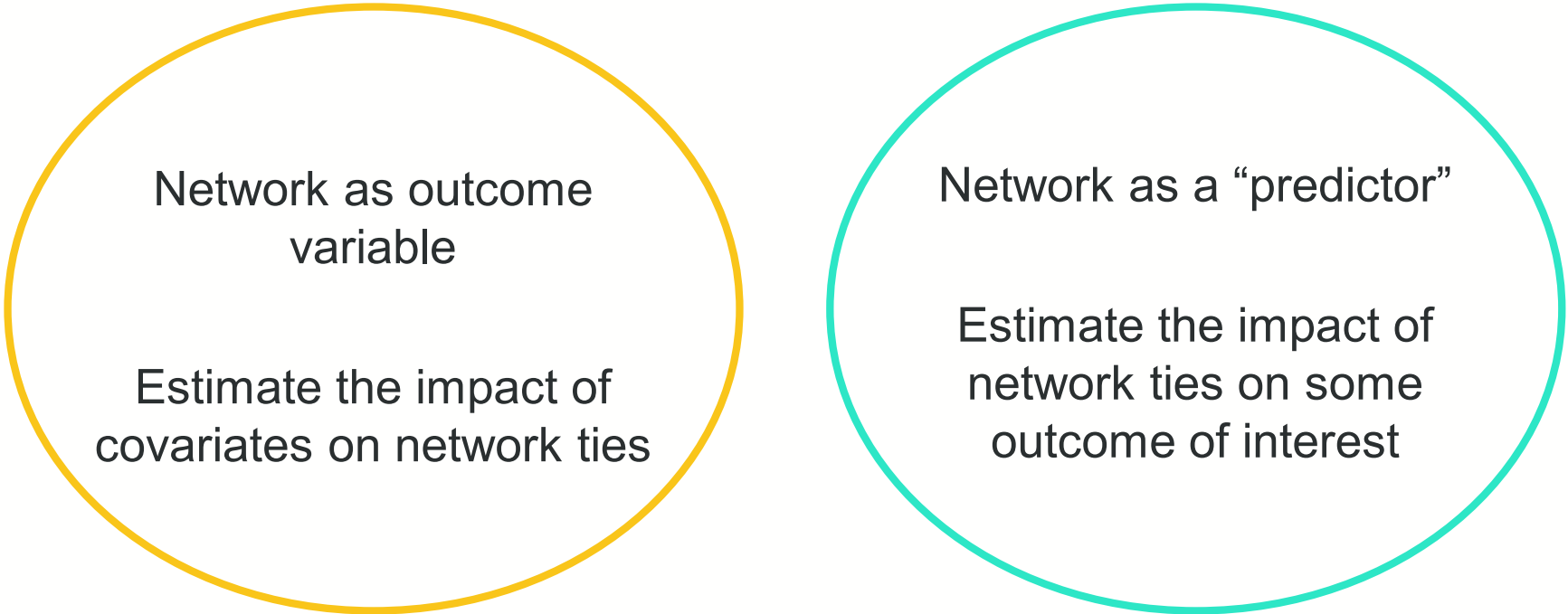
Goals of the Current Study

- Demonstrate the need for more appropriate methodological approaches to student mobility
- Illustrate the use of network analyses in this context using statewide longitudinal data
- Provide guidelines for future methodological studies

What is a Social Network?

- A social network is a set of relations or ties among individuals or entities.
 - Online relationships – e.g. Facebook (Lewis et al., 2008)
 - Friendships and personal relationships (Ennett and Bauman, 1993)
 - Workplace relationships (Krackhardt and Porter, 1986; Spillane et al., 2012)
 - Political alliances (Smith and White, 1992)

Social Network Analyses



The diagram consists of two large circles side-by-side. The left circle has a yellow border and contains text about 'Social Selection'. The right circle has a teal border and contains text about 'Social Influence'. Below each circle is a label: 'Social Selection' for the left and 'Social Influence' for the right.

Network as outcome variable

Estimate the impact of covariates on network ties

Social Selection

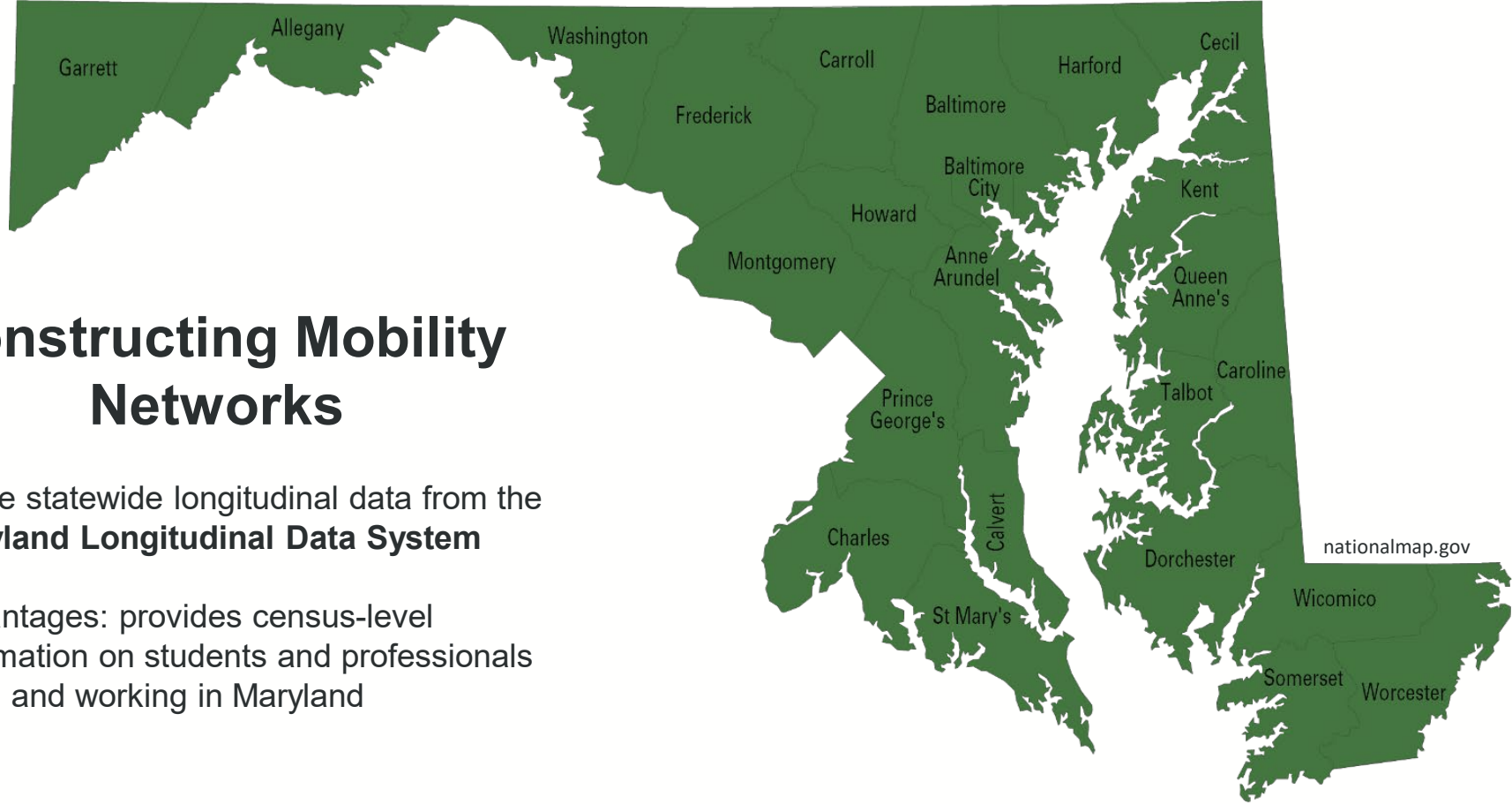
Network as a “predictor”

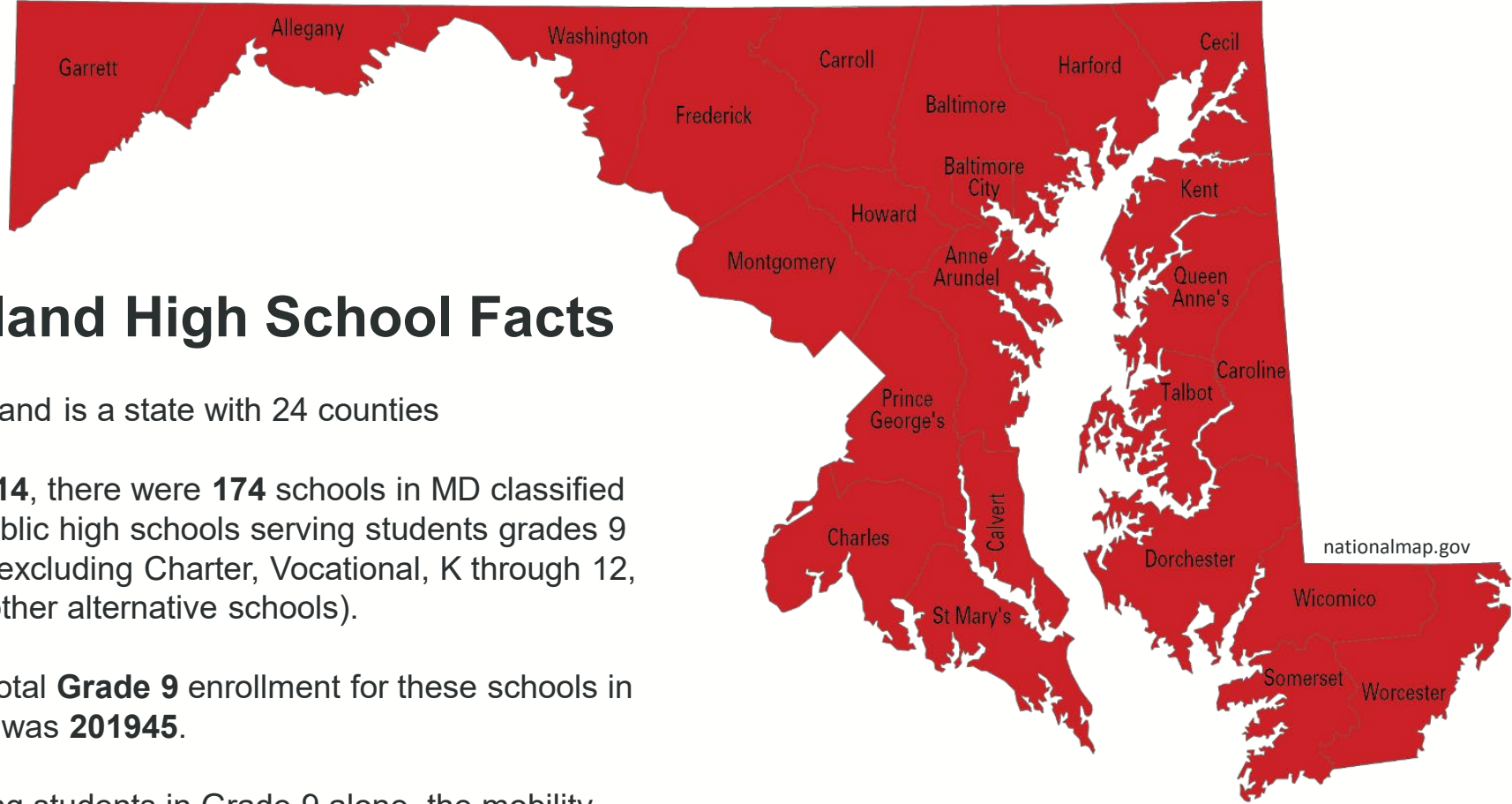
Estimate the impact of network ties on some outcome of interest

Social Influence

Constructing Mobility Networks

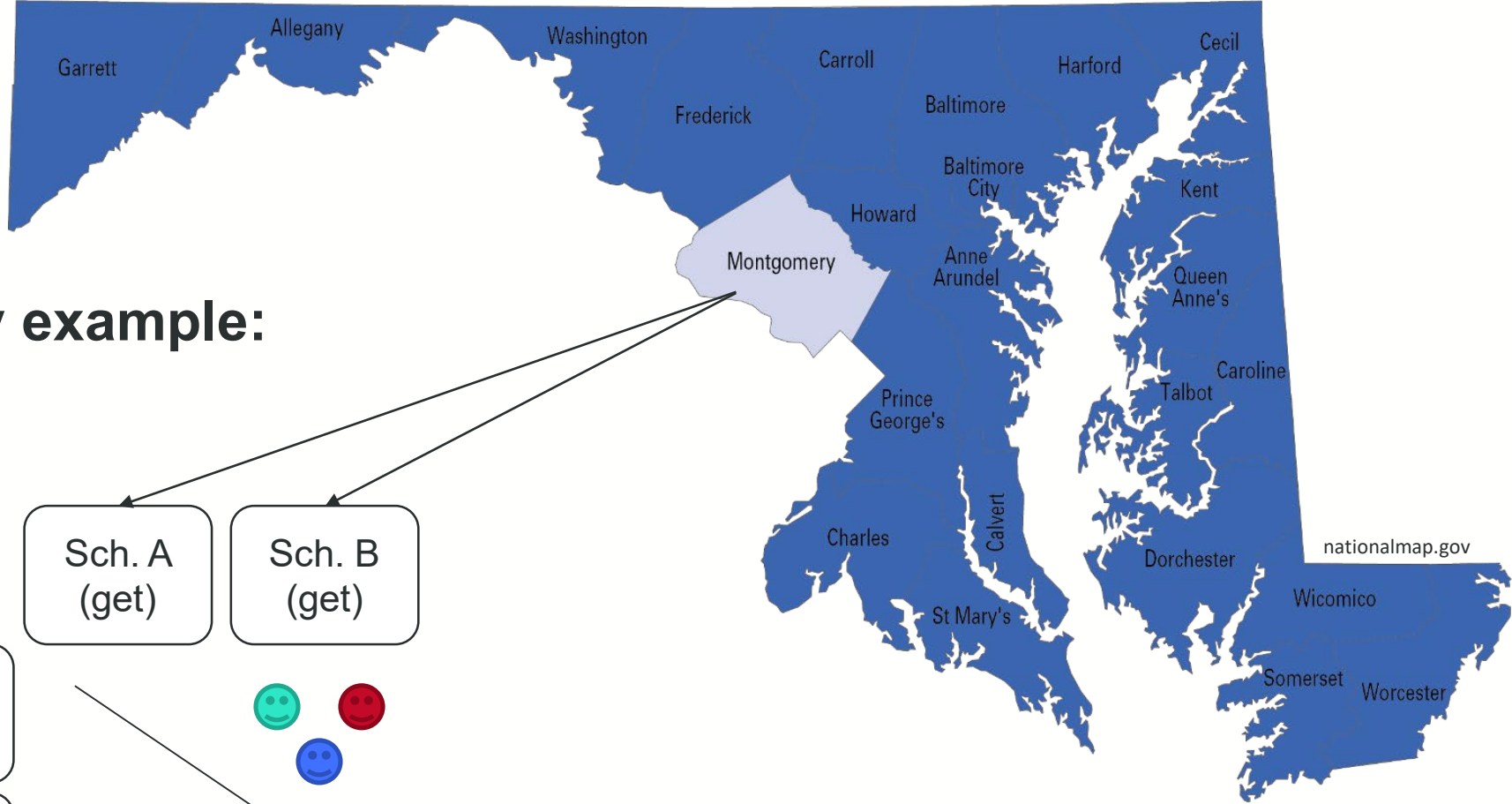
- Utilize statewide longitudinal data from the **Maryland Longitudinal Data System**
- Advantages: provides census-level information on students and professionals living and working in Maryland



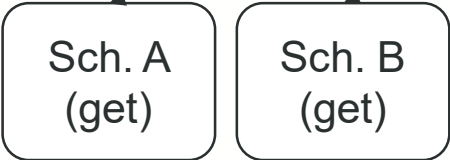


Maryland High School Facts

- Maryland is a state with 24 counties
- In **2014**, there were **174** schools in MD classified as public high schools serving students grades 9 - 12 (excluding Charter, Vocational, K through 12, and other alternative schools).
- The total **Grade 9** enrollment for these schools in 2014 was **201945**.
- Among students in Grade 9 alone, the mobility rate in 2014 was approximately **47%**, with about **16.5%** coming from mid-year entries and about **30.5%** coming from mid-year exits

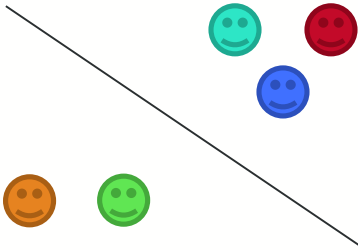


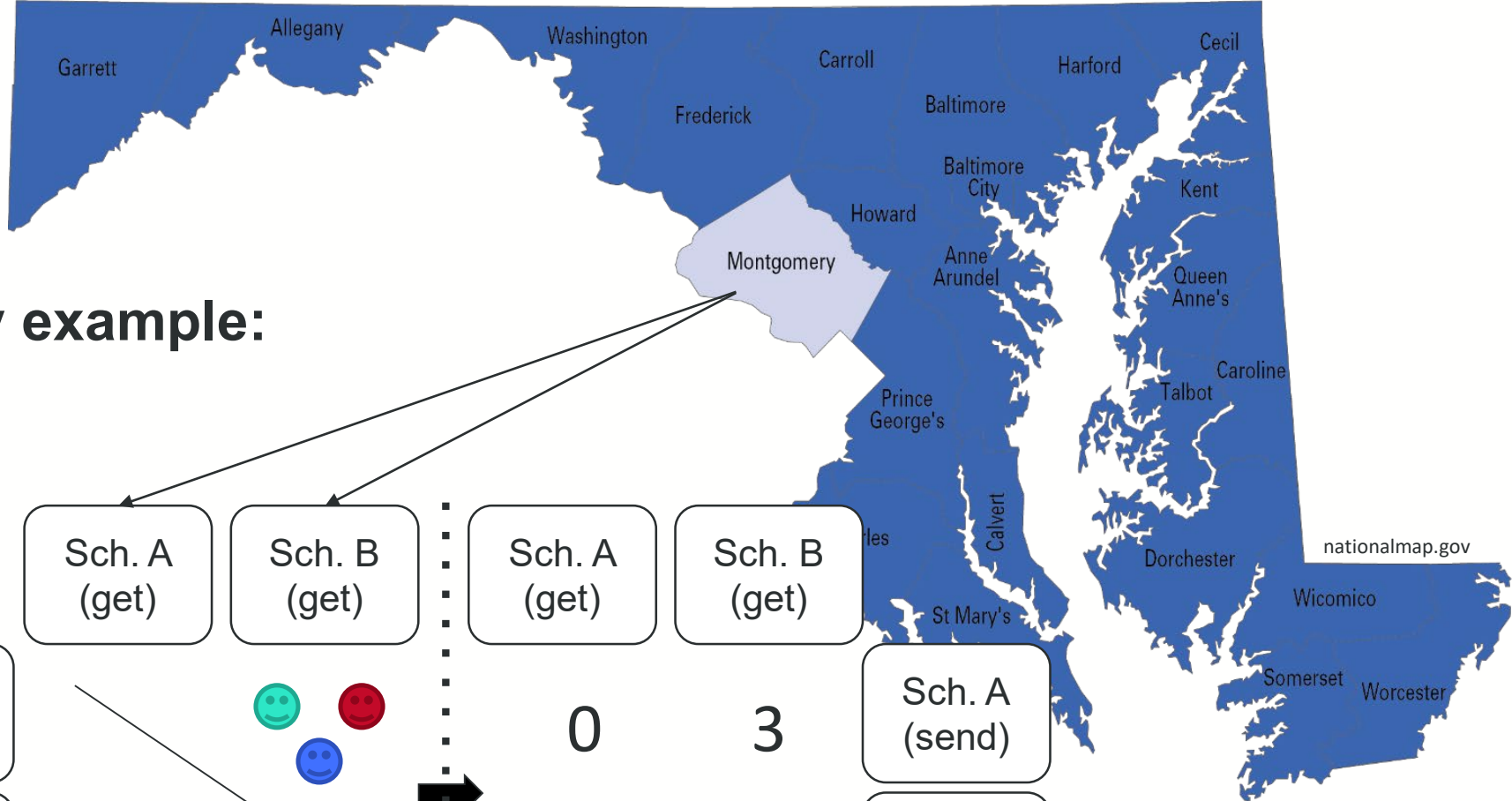
A toy example:



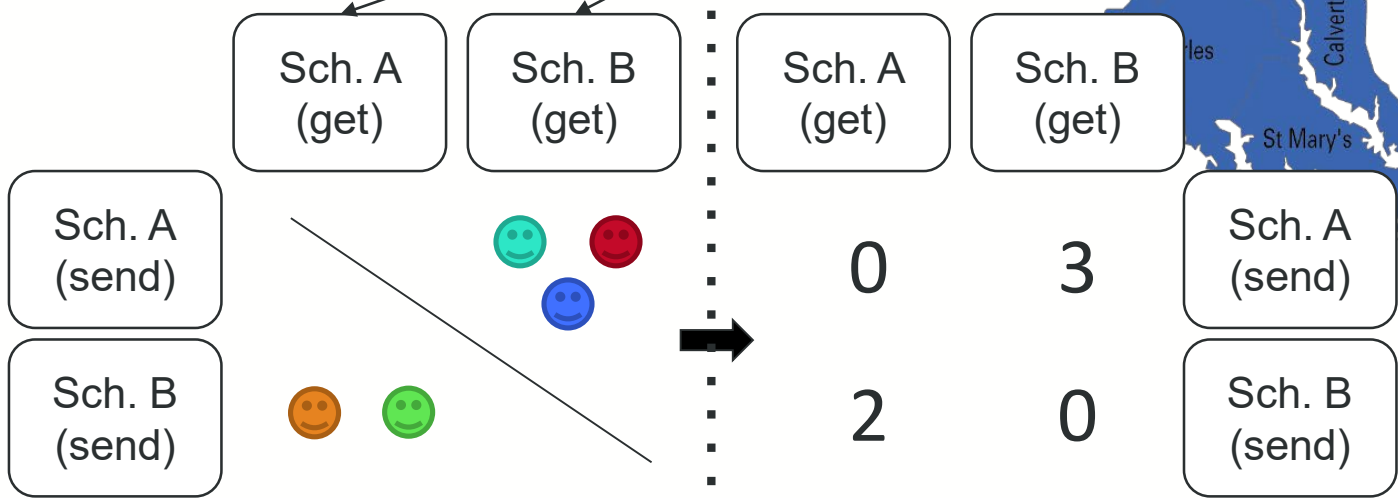
Sch. A
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Sch. B
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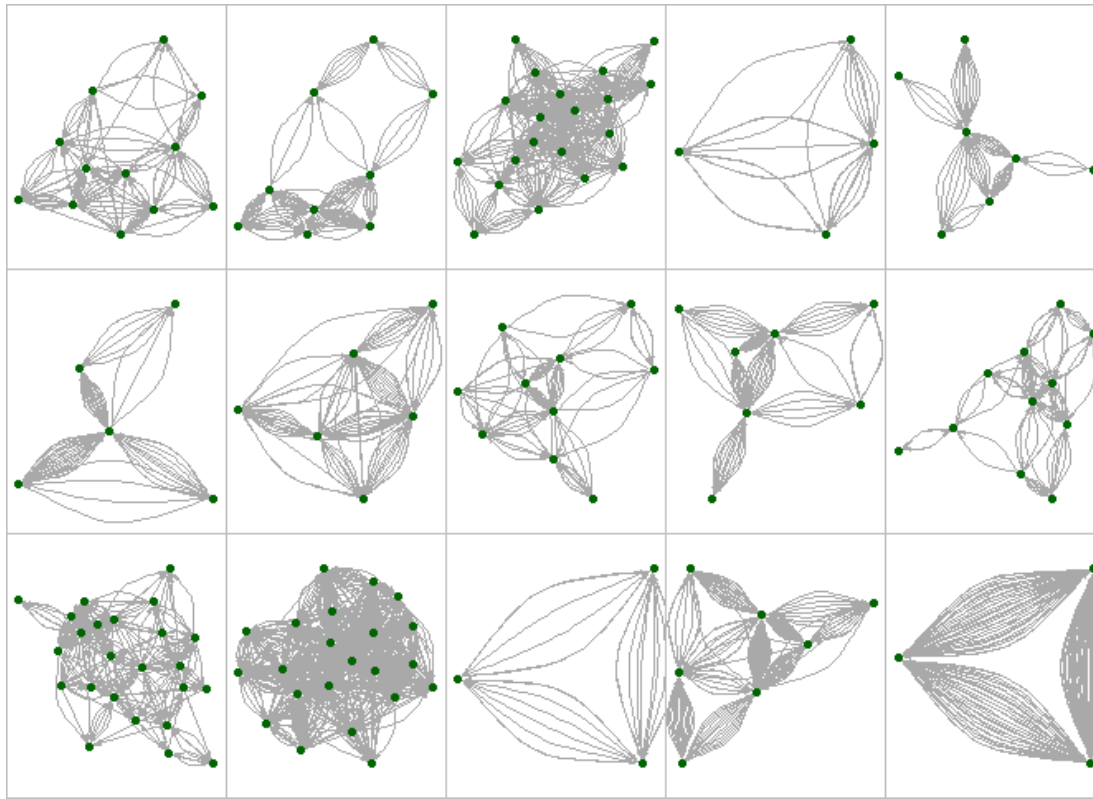




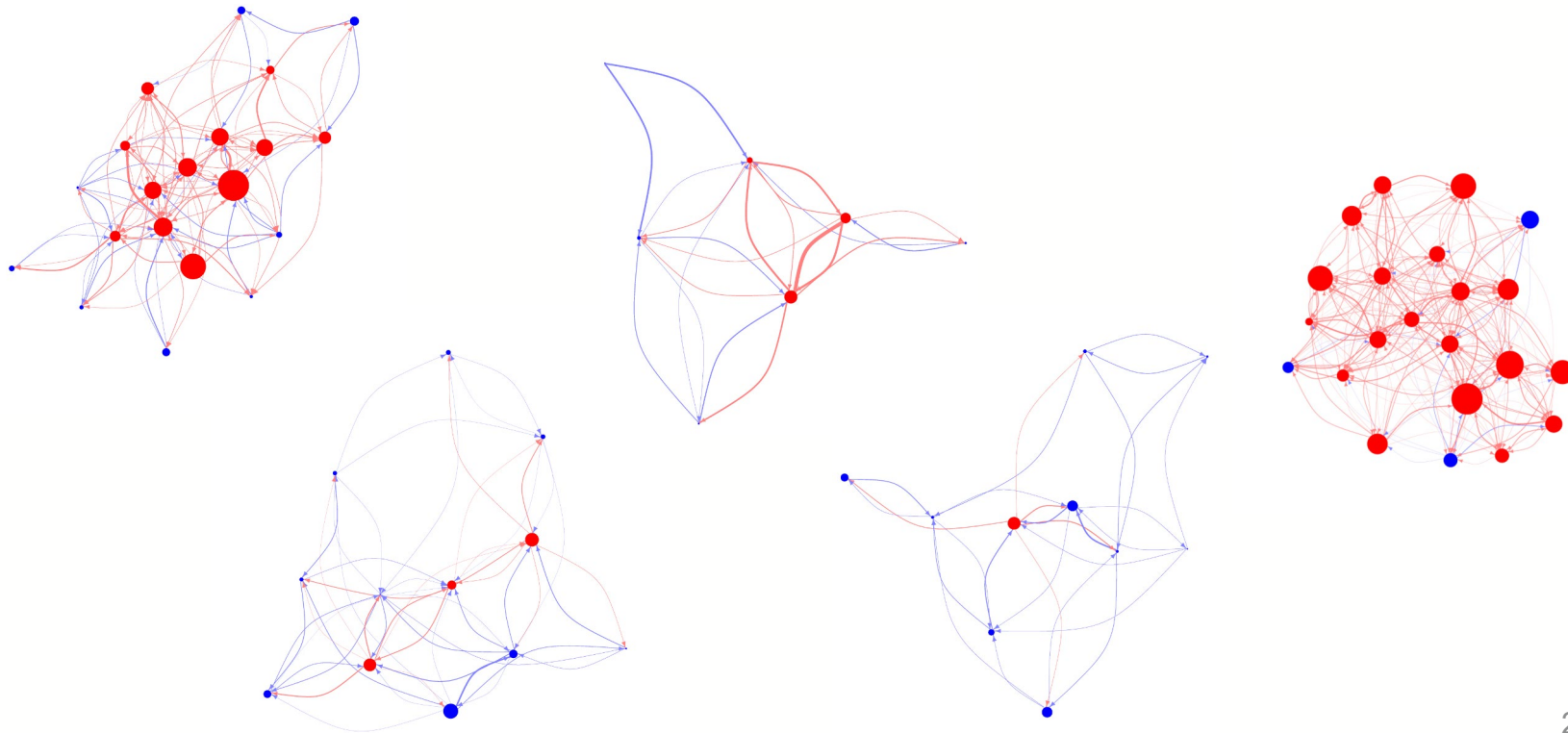
A toy example:



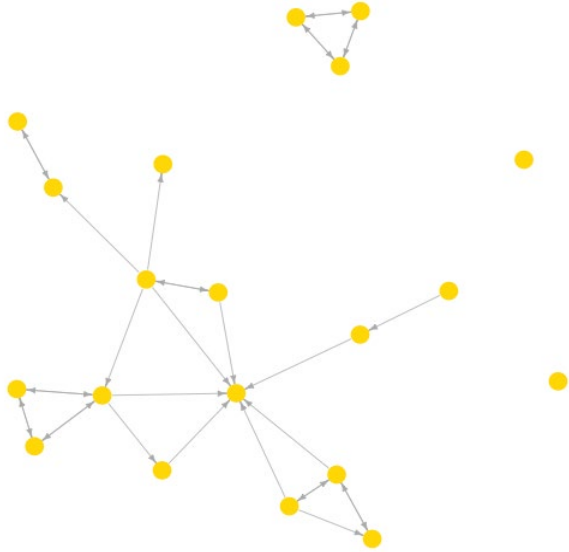
Maryland School Networks



Visualization by Covariates



Descriptives: Node-level disruption



Out-degree: the number of ties sent by a node

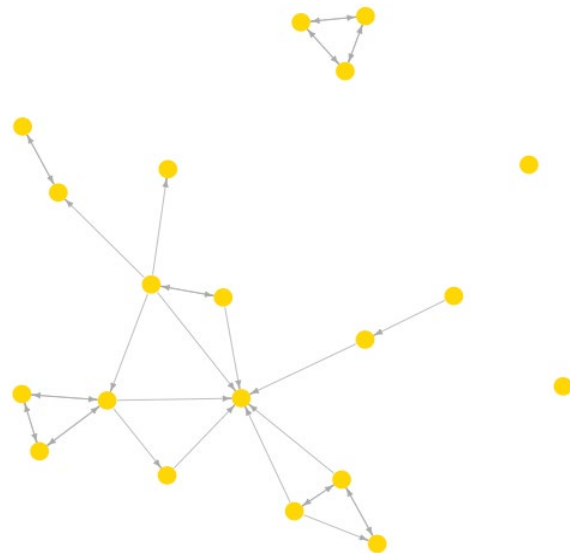
In-degree: the number of ties received by a node

Predicting a Network

To predict binary (ordinal) network ties, we could use logistic (ordinal/probit) regression

Standard GLMs assume independent observations

Network ties are NOT independent.



Latent Space Model (for binary ties)

$$\text{logit}P[Y_{ij} = 1] = \beta X_{ij} - |Z_i - Z_j|$$

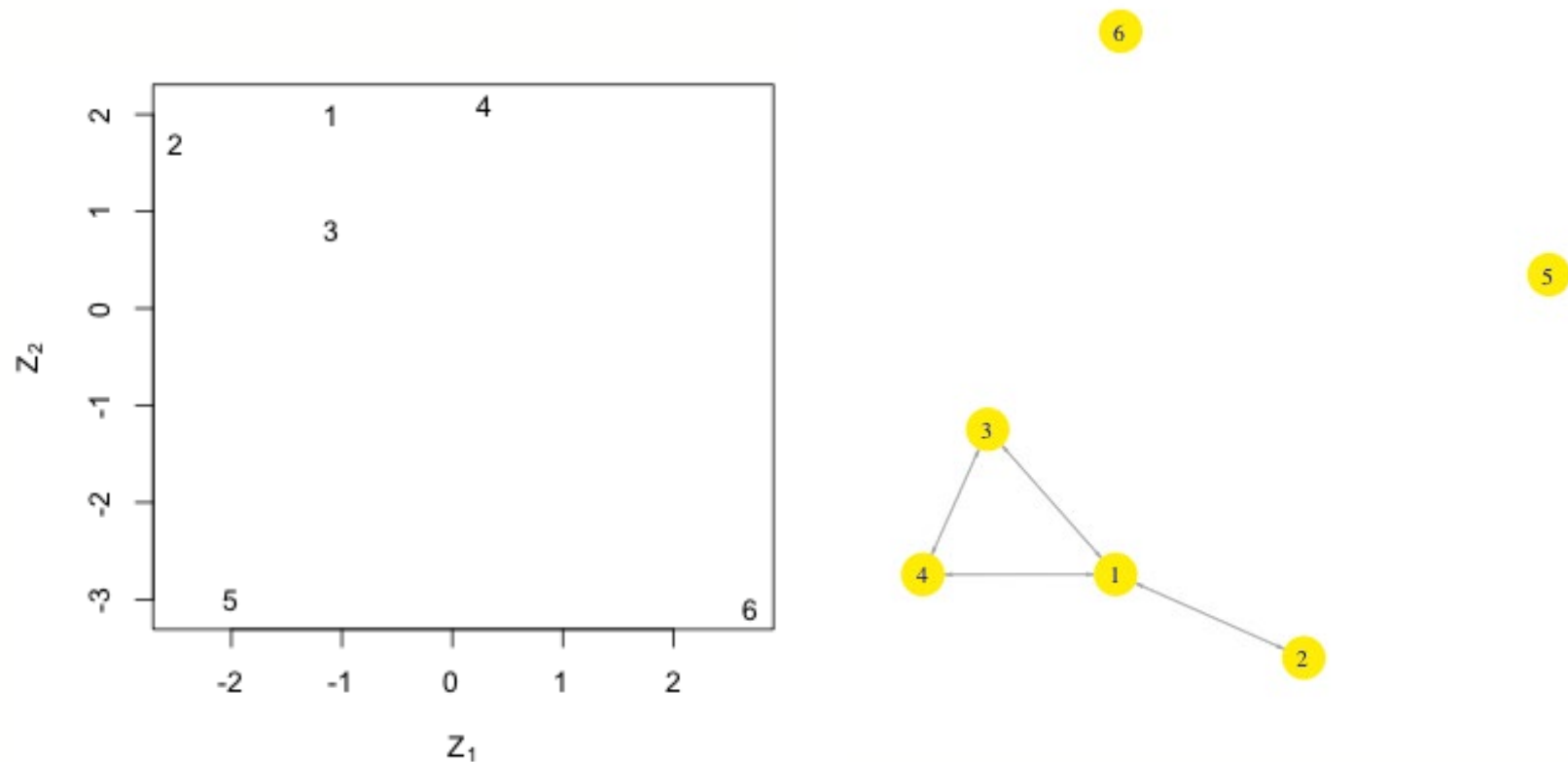
Y_{ij} Is the value of the tie from node i to node j

X_{ij} Is a set of covariates

Z_i Is the latent space position for node i

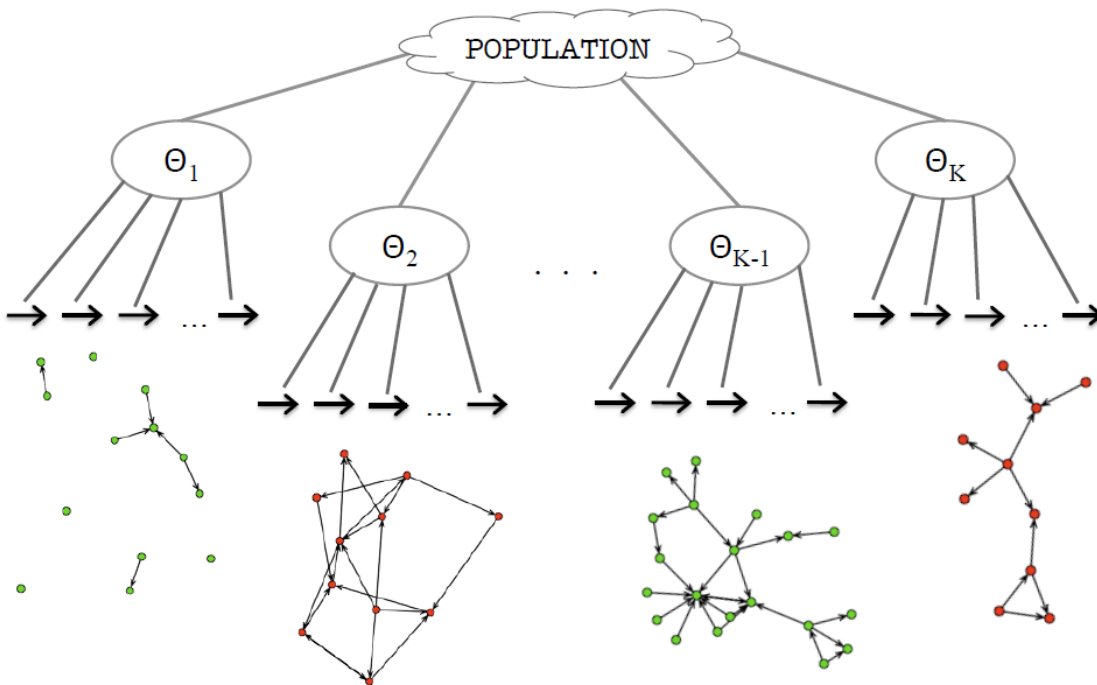
We assume ties are independent conditional on the latent space positions

Latent Space Positions



Hierarchical Latent Space Models

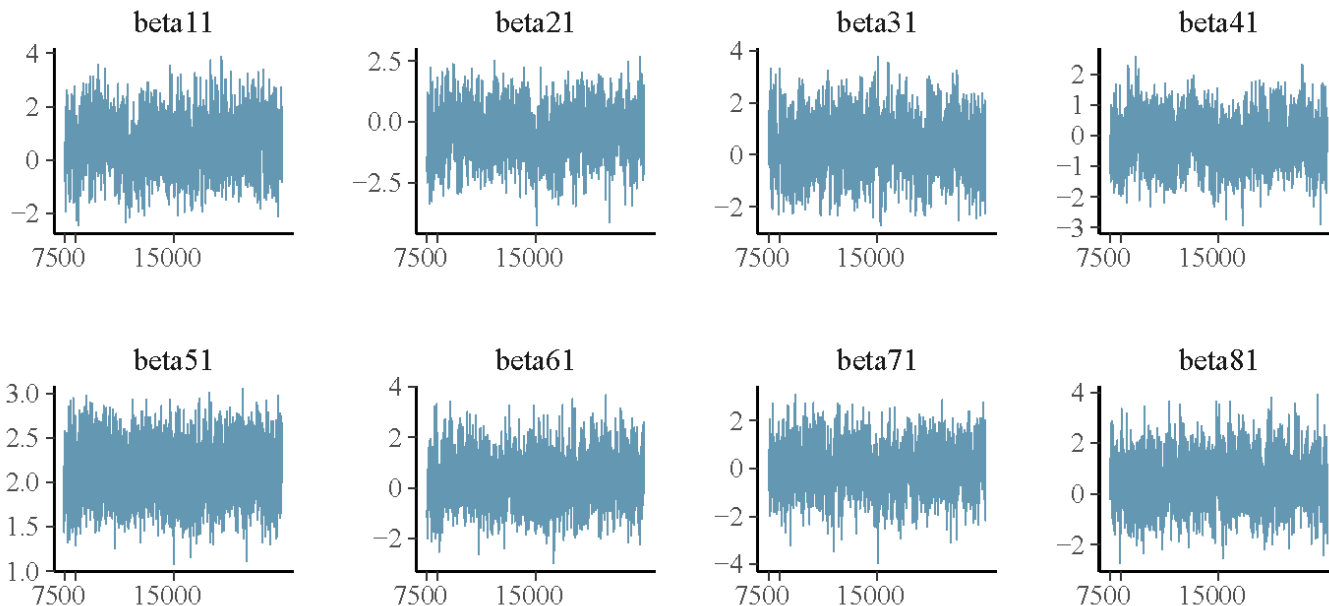
$$P(\mathbb{Y}|\mathbb{X},\Theta) = \prod_{k=1}^K \text{LSM for } Y_k$$
$$(\Theta_1, \dots, \Theta_K) \sim F,$$



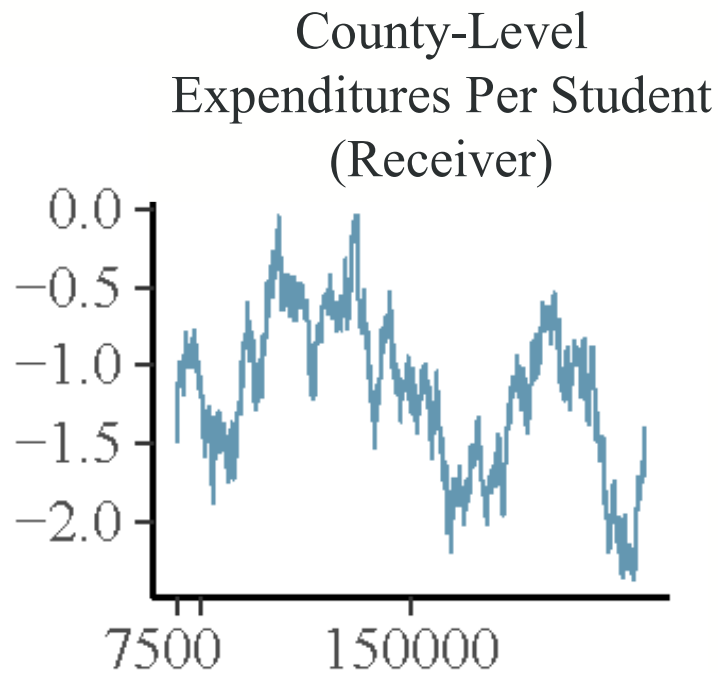
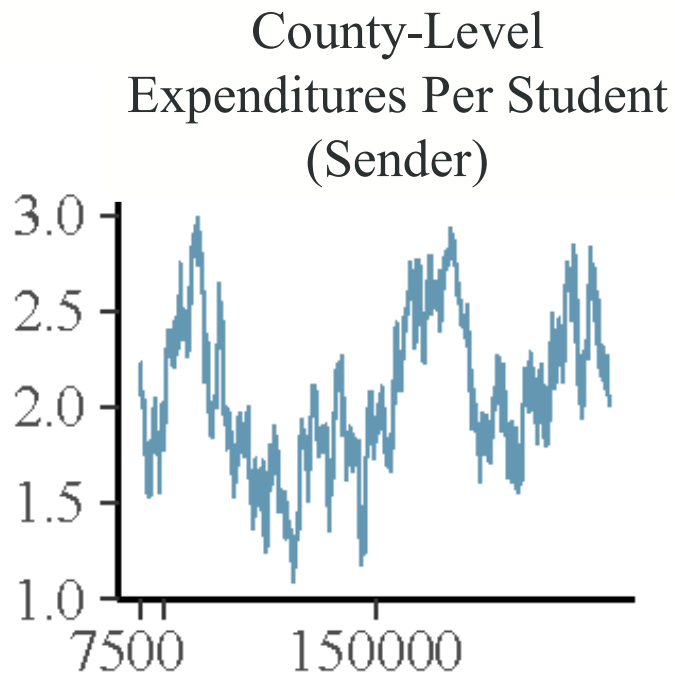
Implementation of the HLSM

- Aggregated student-level, school-level information, and county-level information assessed
 - Aggregated student-level
 - FARMS, suspensions, assessment performance, attendance
 - School-level
 - Previous year graduation and college enrollment rates
 - County-level
 - Previous-year average county wages, expenditures per student

Selected traceplots for the full HLSM

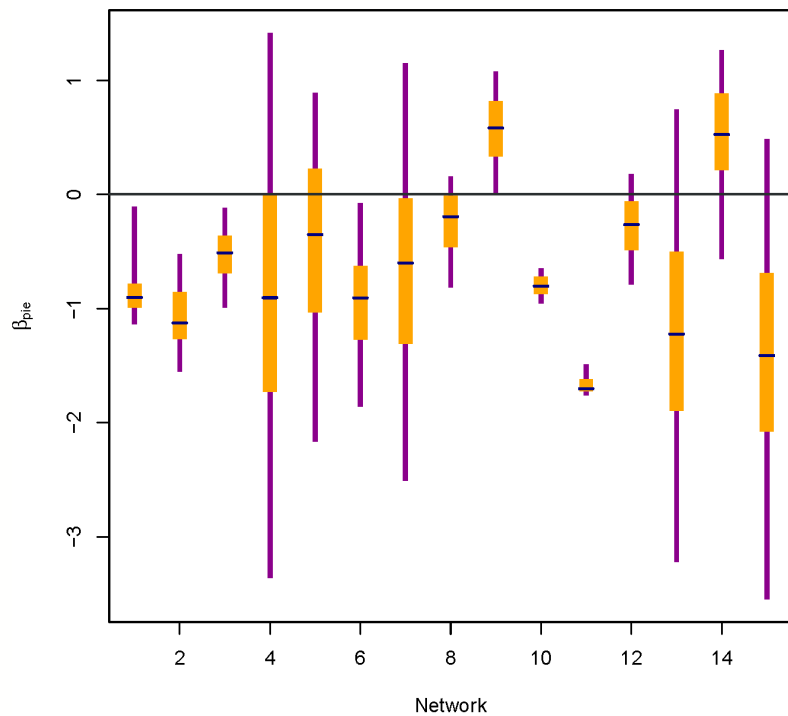


Examples of parameter non-convergence

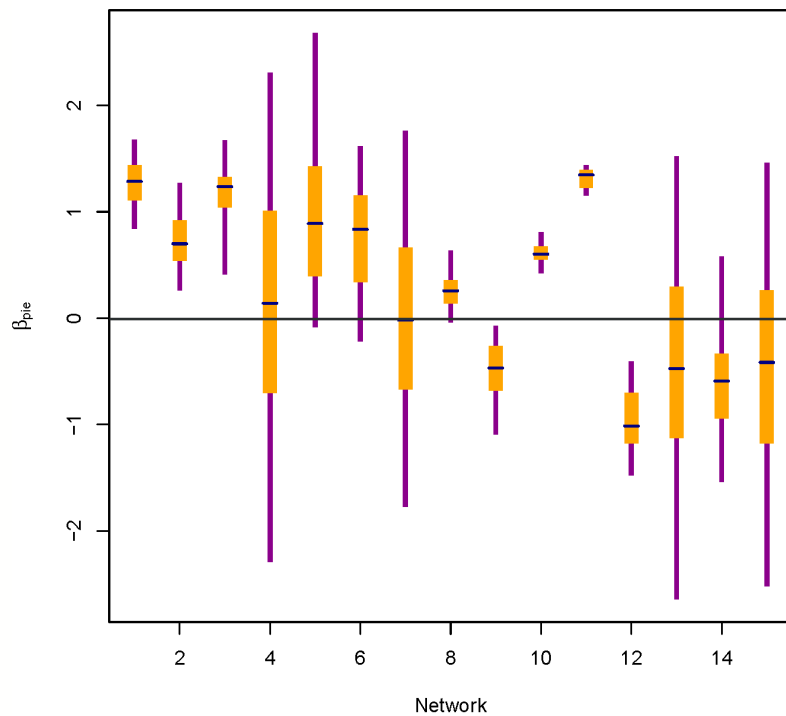


County-Level Expenditures Per Student

(Sender)

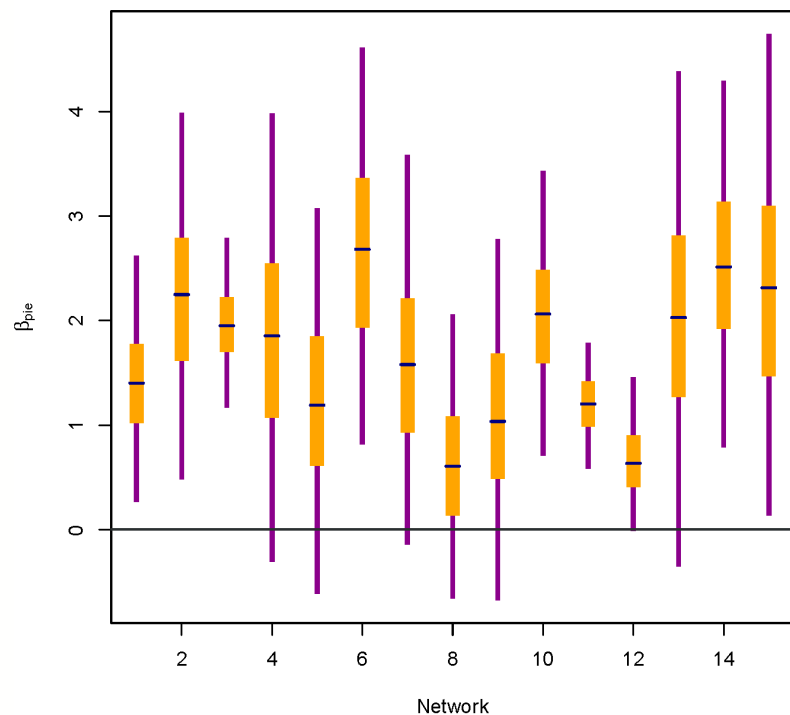


(Receiver)

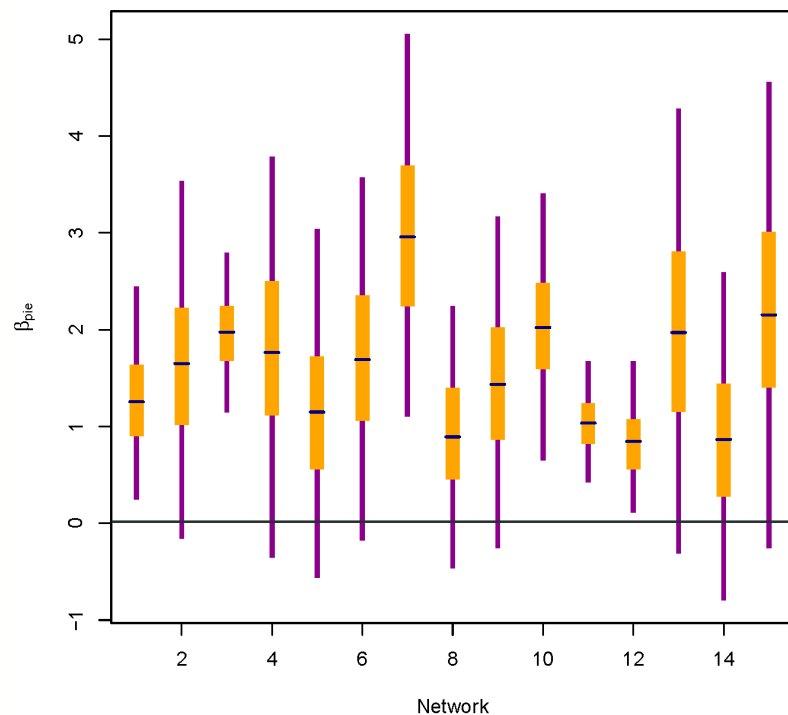


Percent of FARMS Eligible Students

(Sender)



(Receiver)



Results summary

- County-level expenditures have an important school sender/receiver effects above and beyond aggregated student characteristics (more \$\$ = more students received)
- Measures of student poverty remained important predictors of network ties for many counties (higher poverty rates increased the likelihood of observing a tie for both sender & receiver schools)

Where do we go from here?

- Future methodological work needed to investigate the following issues
 - Small cluster-level sample sizes and within-network sample sizes are problematic for estimation
 - Social selection models do not fully place mobility networks in their causal systems
- Explore use of multilevel social influence modeling against MMREMs
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